

Optimal Operating Depth Search for Active Towed Array Sonar using Simulated Annealing

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ABSTRACT

In an active towed array sonar, it is important to find the optimal operation depth. Generally, the optimal depth can be chosen via numerical simulations for all sonar depths and this imposes great burdens of time and cost. In this paper, an efficient approach is proposed to find the optimal depth using the optimisation technique. First, the sonar performance function is newly defined as a measure of how well the active sonar might perform. This function depends on the properties of the ocean environment and the positions of sonar and underwater target. Then, the simulated annealing to find an optimal solution for maximising sonar performance is used. The optimised depth agrees well with the depth obtained from direct searching for all depths of source and receiver combinations, but its computational time is largely reduced.

Keywords: Optimal depth; Active towed array sonar; Probability of detection; Simulated annealing; Sonar performance function

1. INTRODUCTION

The active towed array sonar (ATAS) has been developed to overcome the drawback of the hull-mounted active sonar in the shadow zone. The ATAS consists of a varying depth active source and a towed receiver line array for reception¹. In the ATAS, it is important to select operation depths of the source and receiver, which strongly affects the sonar performance.

Many studies on optimal depth have been done in the field of passive sonar. Ferla and Porter suggest the method for selecting the operation depth of passive sonar². They define the detection radius (DR) to assess the performance of the passive sonar, and use it as a cost function for finding the optimal depth. They identify the optimal receiver depth as the depth where the probability of detection is highest in a range-integrated sense. Since DR is a function with single variable, its maxima can be rapidly found by direct calculation of the cost function. Sha and Nolte predict sonar detection performance for passive sonar³. They propose an analytical receiver operating characteristic expression that characterises the performance of the optimal Bayesian detector in the presence of ocean environmental and source position uncertainty. Gershfeld and Ingenito conduct a numerical simulation study to calculate the receiver depth that would maximise the signal-to-noise ratio for one of several source depths in various shallow water environments⁴. Domingo proposed a mathematical model that focuses on finding the optimal placement for wireless nodes in a three-dimensional

underwater wireless sensor network, whose communication is being affected by the shadow zone⁵.

For the ATAS, previous studies on optimal depth released in the open literatures cannot be found. Since target detection using the ATAS is a bi-static detection, the performance of ATAS is influenced by several parameters such as source depth, receiver depth, target depth, and target range. Thus, it is difficult to find the optimal depths of source and receiver in the ATAS while considering all the parameters.

The goal of this study is to develop an efficient method for finding the optimal depths of an active source and a towed line array in the ATAS using global optimisation algorithm. For optimisation, the sonar performance function (SPF) is formulated based on the sonar equation, which is a measure of how well the ATAS detects the target. The unknown target location is considered probabilistically. The optimal depth of the source and receiver can be found at the peak of the SPF. Rather than directly calculating the SPF for all depths of source and receiver, simulated annealing (SA) optimisation algorithm is applied to find the optimal depth efficiently.

2. SONAR PERFORMANCE PREDICTION

2.1 Sonar performance function

To find the optimal operating depth of source and receiver in ATAS, a useful measure that quantifies the performance of ATAS is necessary. In general, the quantity 'range of the day' is often used as a criterion parameter that represents the sonar performance, based on the probability of detection. Range of

the day indicates a range where the probability of detection is 50 per cent.

In active sonar, the probability of detection is as given by a log-normal distribution² :

$$p_D(SE) = \frac{1}{\sqrt{2\pi\sigma}} \int_{-\infty}^{SE} \exp\left[-\frac{x^2}{2\sigma^2}\right] dx \quad (1)$$

where SE is the signal excess, p_D is the probability of detection, and σ is the standard deviation of SE .

The SE represents the degree to which the source signal stands out from the ambient noise with an SE of 0 dB implying a 50 per cent probability of detection². From the active sonar equation, the SE is given by⁶,

$$SE = FOM - (TL_1 + TL_2) \quad (2)$$

where FOM is the figure of merit and TL_1 and TL_2 are respectively the transmission loss from the source to the target and from the target to the receiver.

Although range of the day provides the physical range obtained from the probability of detection, it remarkably varies with the receiver depth, the target depth, and the range of target and ATAS. Because of such variability, there is an ambiguity in calculating the optimal location with range of the day.

In this study, the SPF is proposed based on the probability density function (PDF) of detection, the PDF of target depth and the PDF of relative range as follows:

$$SPF(Z_R, Z_S) = \int_0^\infty \int_0^D p(Z_T) p(R) p_D(Z_R, Z_S, Z_T, R) dZ_T dR \quad (3)$$

where D is water depth at range R , $p(Z_T)$ is the PDF of target depth Z_T , $p(R)$ is the PDF of relative range, p_D is the PDF of detection, Z_R is the receiver depth and Z_S is the source depth.

Eqn (3) is defined in order to consider both location of target and probability of detection for evaluate the performance of ATAS. When the location of the target is unknown, the probability of detection is useless. In this case, Eqn (3) provides more rational information with the stochastic approach. For a localised target [$p(Z_T) p(R) = \delta(Z_T - Z_0) \delta(R - R_0)$], it is seen that Eqn (3) becomes the probability of detection naturally. It is noted that Eqn (3) is not the cumulative density function (CDF).

The PDFs of the target depth and relative range will depend on the situation being considered. For example, if

the range of the target is known, the PDF of relative range is set to be a delta function with the singularity at specific relative range. Otherwise, it is reasonable to assume that $p(R)$ follows a uniform distribution. The PDFs of the target depth is considered to be a normal distribution since the underwater target has a tendency to use an underwater channel.

Simulation of SPF is performed for the following ocean environment. The sound speed profile and water depth are as given in Fig. 1. The sea floor is composed of silt and clay with the density and sound speed of 1470 kg/m³ and 1585 m/s⁷. The frequency of the source is 3.5 kHz. Transmission losses in Eqn (2) are computed using the acoustic propagation model Bellhop⁸. The standard deviation in Eqn (1) and the FOM in Eqn (2) are respectively set at 8 dB and 130 dB. Figure 2 shows SPF for all source and receiver depths in two cases where the target location is unknown and when only target range is given. The PDF of target depth is considered to be the normal distribution with the mean of 100 m and the standard deviation of 20 m. The PDF of the relative range of target is chosen as the uniform distribution. As shown in Figs. 2(a) and 2(b), the ambiguity surfaces of SPF are different for the two cases. But, it is clear that there is a global optimal location.

To find the optimal location by the direct calculation of

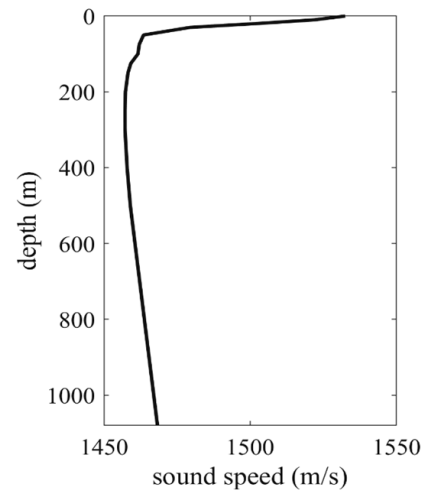


Figure 1. Sound speed profile in the East Sea of Korea during the summer.

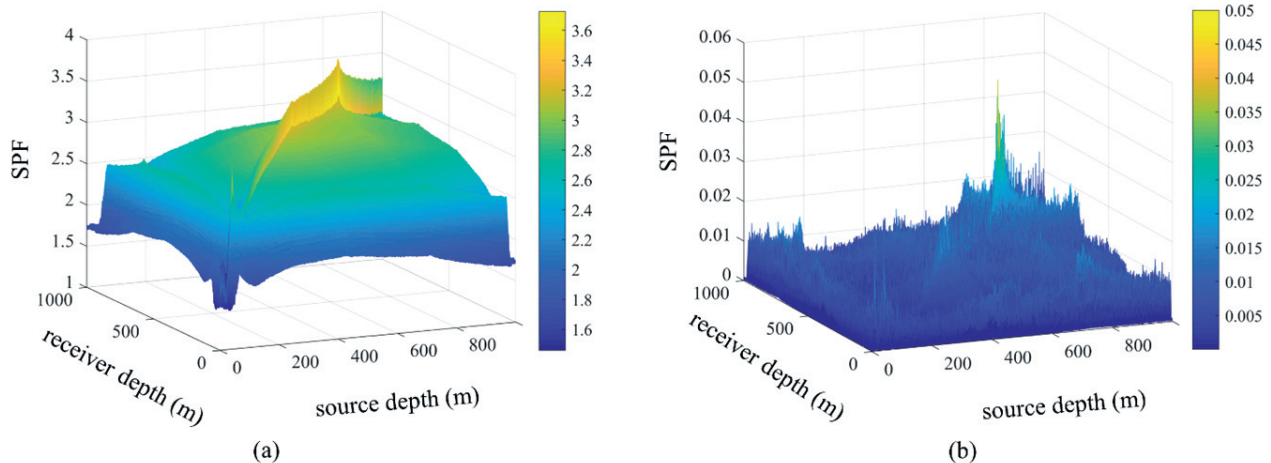


Figure 2. Sonar performance function as a function of receiver depth and source depth when (a) target location is unknown and (b) only target range is known.

Eqn (3) for all source, and receiver depths, much computations would be required. Even if the relative range is known, dividing each depth into 1000 points, a total of 10^6 calculations is needed to obtain the ambiguity surface of SPF. Therefore, it is necessary to introduce an optimisation method to find the optimal locations.

3. OPTIMAL DEPTH SELECTION USING SIMULATED ANNEALING

As described in the previous section, the direct calculation of SPF for all depths of source and receiver is computationally intensive. This section present how to obtain the optimal depth efficiently using a global optimisation algorithm.

3.1 Simulated Annealing for the Optimal Depth

Simulated Annealing (SA) is a global search method that find its inspiration in the physical annealing process studied in statistical mechanics⁹. Since SA is characterised by ease of implementation and fast convergence, it is usually employed as an optimisation method to find an optimal solution for military problem^{10,11}. Basically, SA calculates the object function at a point, and then finds a new point with a higher value of object function with the probability. This process is repeated until the optimal point is reached. The flow chart of the SA algorithm is as given in Fig. 3.

An optimisation is performed for the ocean environment used in the previous section. Figure 4 shows the optimisation result symbolised by red asterisks on the ambiguity function of SPF. It is clear that the optimised depths are consistent with those of the direct calculation of SPF for both cases. However, the time cost is reduced about a thousand times as listed in Table 1.

3.2 Optimal Depth in the East Sea of Korea

Assuming that the active source and receiver array in ATAS are to be operated at the same depth, optimal depths are calculated in the region of East Sea of Korea between 130°E and 135°E longitude and 36°N and 41°N latitude using the proposed method. Sound speed profile at each location is calculated from temperature and salinity data taken in the NOAA World Ocean Database¹².

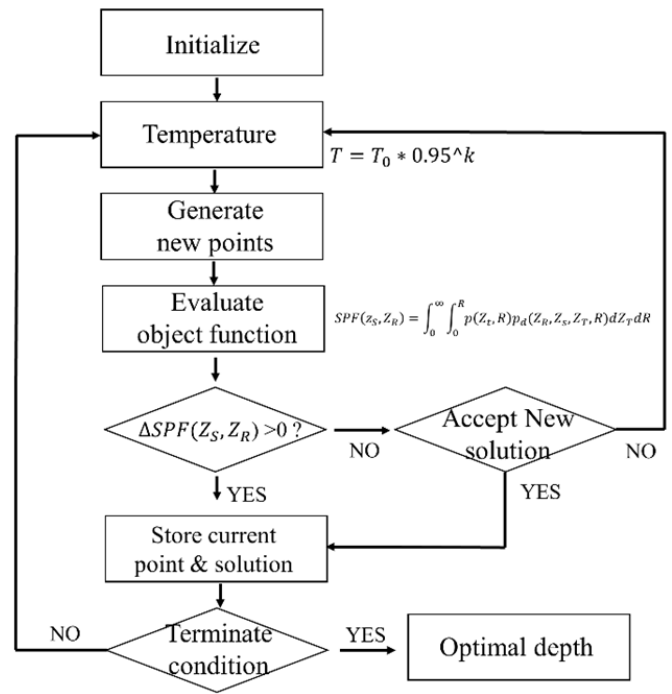


Figure 3. Flow chart of the simulated annealing process.

Table 1. Comparison of the direct calculation and optimisation results.

Case	Item	Number of calculations	Optimal depth (m)	SPF
Fig. 4(a)	SA optimisation	810	728	3.521
	Direct calculation	1,000,000	728	3.520
Fig. 4(b)	SA optimisation	741	215	4.384
	Direct calculation	1,000,000	215	4.387

Bathymetry is obtained from the US Geological Survey (USGS), Global 30 Arc-Second Elevation (GTOPO30) model¹³. Figure 5 shows the bathymetry and the sound speed in the corresponding region. The optimal depths are calculated with 0.25° resolution. Assume that the mean depths of the target are 200 m and 400 m with the standard deviation of 70 m.

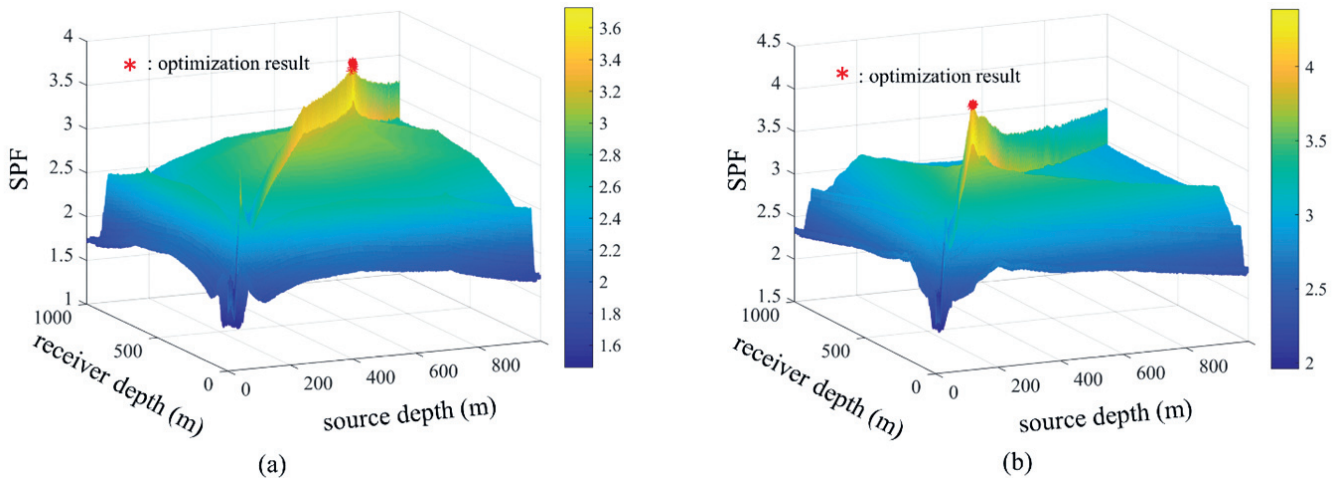


Figure 4. Sonar performance function as a function of receiver depth and source depth with a mean target depth of (a) 100 m and (b) 300 m. The result obtained by the optimisation algorithm is marked with a red asterisk

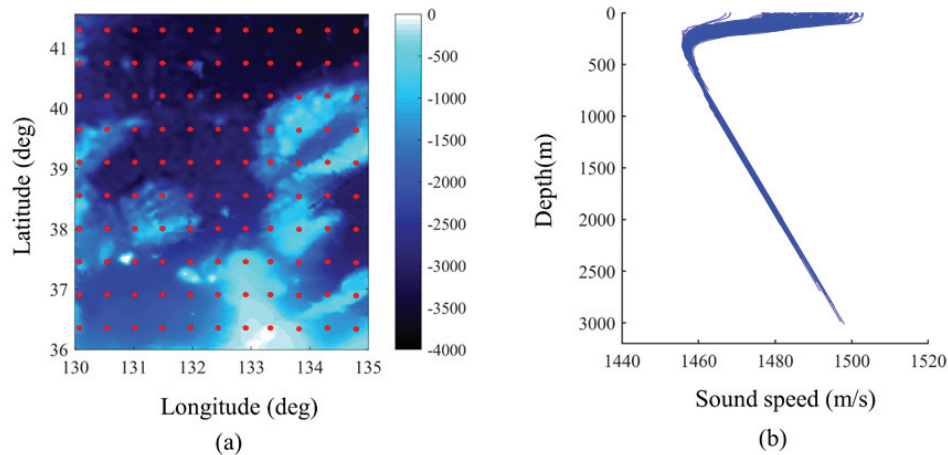


Figure 5. (a) Bathymetry plot for longitude and latitude where red dots represent the ATAS locations for the calculation of its optimal depth and (b) sound speed profiles in the corresponding region.

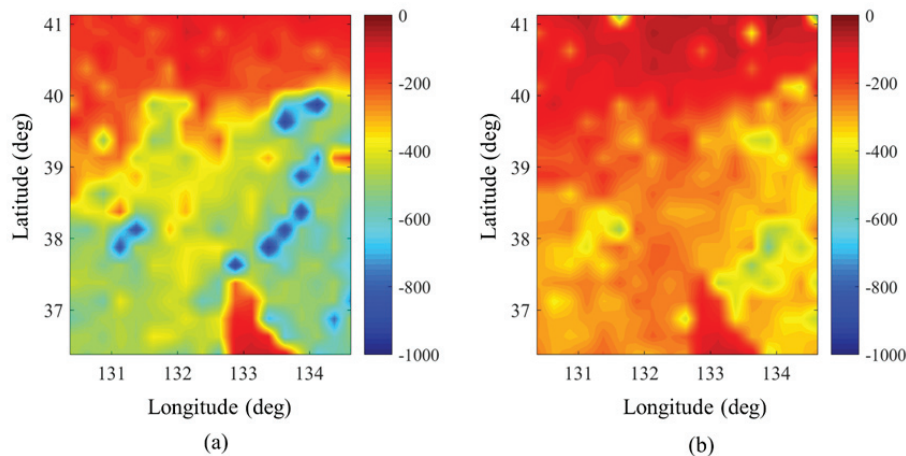


Figure 6. Optimal depth of the ATAS when the source depth and the receiver depth are the same; (a) mean target depth of 200 m and (b) mean target depth of 400 m.

The results are plotted in Fig. 6. Figure 6(a) plots the result for the mean of 200 m and Fig. 6(b) shows the result for the mean of 400 m. The unit of the colour bar is meters. As shown in Fig. 6, the optimal depth depends on the sonar operation region. When the target is moved near the depth of 200 m in the lower region of Fig. 6(a), the sonar has to be operated at greater depth. As the depth of target increases, the optimal depth of the sonar becomes shallower, as shown in Fig. 6(b). Finally, it is noted that it would take about thousand times computation to obtain the same figure as Fig. 6 doing the direct calculations as listed Table 1.

4. CONCLUSIONS

By operating the ATAS at optimal depth in the ocean, the probability of detection of an underwater target will increase. An efficient method is presented to find the optimal depth of ATAS using SA. The SPF is suggested and used to evaluate the sonar performance with the PDFs of detection, target depth, and relative range. The calculations of the proposed method are about one thousand times less than in the direct calculation of the SPF for all depths. With some numerical examples, it is shown that our method can find a global optimal depth and would be a valuable tool in recommending the optimal depth for the ATAS operator.

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