Multi-objective Optimisation of Multi-robot Task Allocation with **Precedence Constraints**

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ABSTRACT

Efficacy of the multi-robot systems depends on proper sequencing and optimal allocation of robots to the tasks. Focuses on deciding the optimal allocation of set-of-robots to a set-of-tasks with precedence constraints considering multiple objectives. Taguchi's design of experiments based parameter tuned genetic algorithm (GA) is developed for generalised task allocation of single-task robots to multi-robot tasks. The developed methodology is tested for 16 scenarios by varying the number of robots and number of tasks. The scenarios were tested in a simulated environment with a maximum of 20 robots and 40 multi-robot foraging tasks. The tradeoff between performance measures for the allocations obtained through GA for different task levels was used to decide the optimal number of robots. It is evident that the tradeoffs occur at 20 per cent of performance measures and the optimal number of robot varies between 10 and 15 for almost all the task levels. This method shows good convergence and found that the precedence constraints affect the optimal number of robots required for a particular task level.

Keywords: Multi-robot task allocation; Multi-robot task sequencing; Foraging tasks; Multi-objective optimisation, Genetic algorithm; Taguchi DOE

NOMENCLATURE

- Task '*i*' with priority p, i=1 to n and p=1 to q T_i^p
- Robot 'j' j=1 to m \mathcal{R}_i
- Destination location k=1 to s \mathcal{D}_{k}
- Number of tasks n_{τ}
- Number of robots $n_{\mathcal{R}}$
- Population size $n_{\mathcal{P}}$
- Number of generations n_G
- Mutation probability
- Crossover probability
- Fitness function
- Task completion time for each task 'i' with priority 'p'.
- $\begin{array}{c} \mathcal{P}_{\mathcal{M}} \\ \mathcal{P}_{\mathcal{C}} \\ f_t \\ \mathcal{C}_t^{\mathcal{T}_t^p} \\ \mathcal{T}_{\mathcal{T}_i}^{\mathcal{R}_j} \\ \end{array} \\ \mathcal{T}_{\mathcal{R}_i^{\mathcal{T}_k}}^{\mathcal{T}_p} \end{array}$ Travel time of robot \mathcal{R}_i from its current location to source location of the task T_i^p
- Travel time of robot \mathcal{R}_i from the source location of task T^p to destination location \mathcal{D}_p

INTRODUCTION 1.

Multi-Robot Systems (MRS) finds real-life applications in automated material handling at warehouses, war front assistance, office support system, environmental cleansing and the robotic scientists are keen in exploring the usage in many other areas. Physical foraging tasks like cooperative object transportation reasonably demand the need for multiple robotic units for task execution. MRS exhibits scalable, fault tolerant and expedited task completion capabilities when compared

to the single standalone robot system. However, a carefully planned task allocation among the individual robotic units plays a significant role in realising the efficiency of the MRS. Multi-robot task allocation (MRTA) problems are to determine the best possible assignment of robots to each task and to find the sequence of the tasks for each of the robot to minimise the total task completion time. An improper allocation of the robots to such tasks would undoubtedly lead to extended completion time and excess resource utilisation. At times it may end in a deadlock situation, when two jobs may be waiting invariably for two different robots waiting for each other. Apart from allocating the robots to a given set-of-tasks, finding the optimal $n_{\mathcal{R}}$ to be deployed would help the system to operate at minimal cost and with high efficiency.

2. **RELATED WORK**

The detailed classification¹ of MRTA problems available in the literature are based on

- Type of robots (single task (ST) vs. multiple task (MT) (i) robots)
- (ii) Type of tasks (single-robot (SR) task and multi-robot (MR) tasks), and
- (iii) Type of assignments (instantaneous assignment (IA) and time-extended assignment (TA).

Further classification² on time-extended assignments includes time windows, synchronisation and precedence constraints. Having such a broad classification, researchers attempt to solve numerous problems in the MRTA domain. The

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problem complexity also varies with the application for which the robots are deployed and also based on the robot capabilities. Ultimately, task allocation is done to execute the task on hand with available robots. However, the task allocation depends significantly on the objectives that the user tries to optimise. Different objectives were considered such as minimisation of energy expenditure³, maximisation of utility value^{4,5} of robots, minimisation of task completion time^{6,7}, minimisation of distance travelled by the robots^{8,9} or at times if the robots speed are variable, robot travel time considered. Some problems were solved are in single objective in nature some are multi-objective types. Some multi-objective optimisation approaches considered rewards, path cost and damage to the vehicle as objectives¹⁰ and used a weighted technique to obtain a solution.

A review of MRTA algorithms and comparison of market-based approaches along with the simulated annealing and Genetic algorithm¹¹ concludes that the latter performs well. Algorithm time complexities between Hungarian Algorithm and GA were compared¹² and found that GA performs better while scaling up robotic units. GA with the different mutation parameters were analysed¹³ and found the inversion mutation perform better when compared to the swap mutation. Other related works for MRTA includes Ant colony optimisation based task allocation¹⁴ and comparison between Tabu search, Simulated Annealing and random search methods¹⁵ for different tasks. Social welfare based task allocation method¹⁶ minimises the resource consumption and maximises the completion rate of tasks. Probabilistic task allocation method¹⁷ under uncertain costs conditions and with risk preference concludes that risk has no effect on optimal assignment but, uncertainty plays a significant role in deciding the optimality. The two-level distributed method¹⁸ with the centralised method for production planning and task allocation using multiple robots shows that the decentralised approach invites much production cost due to information scarcity. But the centralised method involves higher robot distance cost but still proved to be superior. Decentralised sub-planning and centralised optimisation of task allocation procedure¹⁹ reduces the burden on the task manager, but the computation complexity of this method increases as the robots are scaled up. A general classification of solution methodologies for MRTA problems includes centralised and decentralised approaches. Decentralised approaches outperform centralised methods in finding the solutions to the problem in a short time. Whereas, centralised approaches perform well in the global optimisation grounds.

The [ST-MR] configuration is addressed by very few researchers^{20,21} and the use of conventional optimisation methods to solve problems of [ST-MR] setup involves many variables, and hence it is computationally intensive to find a solution. Moreover, the effect of precedence constraints in [ST-MR] problems and objectives related to robots such as a number of robots utilised, waiting time and idle times of robots were given least importance when compared to task-related goals. This paper proposes an evolutionary optimisation technique to find the solution in a centralised approach to MRTA problem considering, precedence relationship including both robot

centric and task-centric objectives.

The following are the notable contributions of this work:

- (i) GA based methodology for MRTA problem with new combination of multiple objectives.
- (ii) Statistical method to identify the best levels for GA parameters for solving MRTA problems.
- (iii) Explored a way to identify the optimal number of robots for a given set-of-tasks with precedence constraints.

3. PROBLEM STATEMENT

At any given instant of time, set-of-tasks precedence are represented with constraints as $\mathbb{U}_{T} = \left\{ T_{1}^{1}, T_{2}^{1}, \dots, T_{a}^{1}, T_{1}^{2}, T_{2}^{2}, \dots, T_{b}^{2}, \dots, T_{1}^{q}, T_{2}^{q}, \dots, T_{y}^{q} \right\}$ where a, b and y are n_{τ} in each precedence level P=1 to q. Homogeneous robots are to be allocated to identical foraging tasks at various locations. Each prioritised foraging task T_i^{P} requires *m* robots for its completion. Let the set of homogeneous robots available for completing the tasks are $\mathbb{U}_{R} = \{\mathcal{R}_{1}, \mathcal{R}_{2}, \dots, \mathcal{R}_{n}\}$. The source location of tasks (x_T^s, y_T^s) and the n_R required to complete the task are known in advance. Each allocated task will have a group of robots that get assembled at the site and transport the material to the nearest destination point $(x_{T_i}^D, y_{T_i}^D)$. Once the task is completed, the robot is free to take the next allocated task. It is assumed that the robot moves at a speed of 2 unit distance per time unit. at no load condition and one unit distance per time unit, at the loaded state.

This paper considers the following four minimisation objectives for optimisation.

- (i) Total task completion time C_{t}^{T} time-taken for completion of all the task in all the priorities
- (ii) Aggregated robot travel time $T_i^{\mathcal{R}}$ total travel-time taken by all the robots to complete all the tasks
- (iii) Aggregated robot waiting time $W_i^{\mathcal{R}}$ if a task is a multirobot task, then the robots that arrive at task site have to wait until all the other robots required to perform a task arrives at the site. Addition of all such waiting time, of all the robots and for all the instances, is Aggregated Robot Waiting Time.
- (iv) Aggregated robot idle time $\mathcal{I}_t^{\mathcal{R}}$ an individual robot may go unallocated between tasks due to precedence constraints. Time for which the robot stays unallocated is considered as robot idle time. Aggregated idle time of all the robotic units is considered as aggregated robot idle time.

The simulated environment of size 100 m x 100 m is considered for this study. A maximum of 20 robots was deployed to complete 40 multi-robot foraging tasks with precedence constraints. Figure 1 shows robots, tasks with a number of robots required for completion and the destination locations.

4. PROPOSED METHODOLOGY

MRTA problem is one with significantly large solution space and hence, it is computationally intensive for finding the optimal solution. Non-conventional optimisation methods like genetic algorithm (GA) is a better choice for solving problems

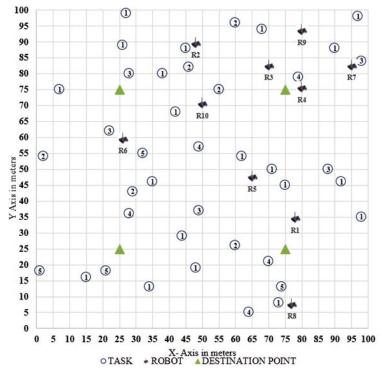


Figure 1. Environment: a sample view.

with a large solution space. GA works better in avoiding local optima and searches for global optima by a random search strategy. Application of elitism concept in GA preserves the best individuals.

4.1 Fitness Function

GA requires a fitness function for selection of the best solution among the various randomly generated ones. The fitness function for a multi-objective optimisation is represented as a single weighted objective function. The multi-objective fitness function is given as Eqn. (1).

$$f_{t} = \lambda_{1} \mathcal{C}_{t}^{T} + \lambda_{2} T_{t}^{\mathcal{R}} + \lambda_{3} \mathcal{W}_{t}^{\mathcal{R}} + \lambda_{4} \mathcal{I}_{t}^{\mathcal{R}}$$
(1)

where $\lambda_1, \lambda_2, \lambda_3$ and λ_4 are the weights of the respective functions. Weighted sum approach to solve multi-objective optimisation is one of the computationally efficient procedures in generating non-dominated solutions^{22, 23}. Some studies^{24, 25} obtained best results by using equal weights to solve the multiobjective problems. This work considers a generalised task allocation problem with multiple objectives but not oriented to any specific application. Hence, same weight is considered for multiple objectives. However, when the problem is solved to a specific application appropriate weights may be assigned to multiple objectives.

The following steps were performed to evaluate C_t^T

Step 1: Arrange tasks based on precedence constraints.

Step 2: Divide the tasks within the same precedence constraints into two sets \mathbb{C}_T and \mathbb{D}_T . Where set \mathbb{C}_T consists of tasks that do not contain any resource (robot) constraint and can be performed in parallel. All the remaining tasks were taken into the set \mathbb{D}_T . The robots required for completing the task in the set \mathbb{C}_T were kept in the set \mathbb{E}_R and the remaining robots are kept in \mathbb{F}_R .

Step 3. Arrange the tasks in set \mathbb{C}_T in ascending order

based on the required time to complete the task. Task completion time for each task 'i' with priority 'p' denoted by $C_i^{\mathcal{I}_i^p}$ and calculated based on travel time. The travel time in Eqn (2) consists of two components (i) no-load travel time of robot \mathcal{R}_j from its current location to source location of the task \mathcal{T}_i^p denoted by $T_{\mathcal{I}_i^p}^{\mathcal{R}_j}$ (ii) loaded travel time of robot \mathcal{R}_j from the source location of task \mathcal{T}_i^p to destination location \mathcal{D}_k indicated by $T_{\mathcal{R}_j}^{\mathcal{I}_p}$

$$\mathcal{C}_{t}^{\mathcal{T}_{i}^{p}} = argmax\left(T_{\mathcal{T}_{i}^{p}}^{\mathcal{R}_{j}} * \mathcal{A}_{j}^{\mathcal{T}_{i}^{p}}\right) \forall j + T_{\mathcal{D}_{k}}^{\mathcal{T}_{i}^{p}}$$
(2)

where $\mathcal{A}_{j}^{\mathcal{T}_{i}^{p}} = \begin{cases} \text{l if task } \mathcal{T}_{i}^{p} \text{ is allocated to Robot } j \\ 0 \text{ otherwise} \end{cases}$

Step 4. Delete all the completed task from the set \mathbb{C}_{T} and add the particular robots used for the task back to set \mathbb{F}_{R}

Step 5. Verify the availability of robots in the set \mathbb{F}_R to perform tasks in set the \mathbb{D}_T and if it is so, it was inserted in the ascending order based on $C_t^{T_t^p}$ in the set \mathbb{C}_T accordingly robots from the set \mathbb{F}_R is added to the set \mathbb{E}_R .

Step 6. Repeat steps 1 to 3 until all tasks in a particular priority are completed.

Step 7. The completion time for the last job was the completion time for the first priority tasks.

Step 8. Repeat steps 1 to 5 until completion of all the tasks.

Step 9. The completion time of all the tasks was calculated as follows

After performing the above steps C_t^T , T_t^R , W_t^R and I_t^R is calculated by Eqns. (3), (4), (5), and (6) respectively

$$\mathcal{C}_{t}^{T} = \sum_{p=1}^{q} \sum_{i=1}^{m} \mathcal{C}_{t}^{T_{i}^{p}}$$
(3)

$$T_{t}^{\mathcal{R}} = \sum_{p=1}^{q} \sum_{i=1}^{n} \sum_{j=1}^{m} T_{T_{i}^{p}}^{\mathcal{R}_{j}} * \mathcal{A}_{j}^{T_{i}^{p}} + \sum_{p=1}^{q} \sum_{i=1}^{n} \sum_{j=1}^{m} \sum_{k=1}^{s} T_{\mathcal{R}_{j}^{p_{k}}}^{T_{i}^{p}} * \mathcal{B}_{k}^{T_{i}^{p}}$$
(4)

where $\mathcal{B}_{k}^{\mathcal{T}_{i}^{p}} = \begin{cases} \text{i if task } \mathcal{T}_{i}^{p} \text{ is allocated to Destination } \mathcal{D}_{k} \\ 0 \text{ otherwise} \end{cases}$

$$\mathcal{W}_{t}^{\mathcal{R}} = \sum_{p=1}^{q} \sum_{i=1}^{n} \sum_{j=1}^{m} \mathcal{W}_{\mathcal{R}_{j}}^{\mathcal{T}_{i}^{\mathcal{P}}}$$
(5)

where $\mathcal{W}_{\mathcal{R}_i}^{\mathcal{I}_i^p}$ is the waiting time of robot \mathcal{R}_i at task \mathcal{I}_i^p

$$\mathcal{I}_{t}^{\mathcal{R}} = \sum_{j=1}^{m} \mathcal{J}_{\mathcal{R}_{j}}$$
(6)

where $\mathcal{J}_{\mathcal{R}_j}$ is the total idle time of robot \mathcal{R}_j between various tasks.

4.2 Chromosome Design

In GA, the chromosome represents the actual solution to the problem. So each chromosome provides the allocation of a set of robots to all the tasks. The chromosome design is of a matrix form which contains, n rows and m columns. The first row denotes the tasks arranged according to the priorities. When there are m tasks with p priorities and a, b and y number of tasks in each priority respectively, the total number of tasks equals the sum of the number of tasks in each priority. The maximum number of rows in the matrix is equal to the maximum number of robots required for any task. So the first row of each column is allocated to a task, and its following rows are allocated to the robots necessary for the task. A sample chromosome is as shown in Fig. 2. A randomly generated chromosome may offer an infeasible solution (i.e., the same robot is allocated more than once for a particular task). The random permutation generation method used in this work ensures the generation of a feasible chromosome (i.e., without assigning the same robot for any specific task).

Task arranged as per priority

	T_1^1 °	T_2^1	T_3^1			T_a^1	T_{1}^{2}	T_{2}^{2}			T_b^2			T_1^q	T_2^q				T_y^q
.[R_1	R_1	R_3	-	-	R_2	R_4	R_3	-	-	R_1	1-1	×.	R_4	R_1	-	-	-	R_1
m	R_3	R_2	R_4	-	-	-	R_1	-	-	-	R_2	. i-	-	-	R_5	1-1	-	-	R ₃
Robots Required for each task																			

Figure 2. Chromosome design.

4.3 Crossover

In GA, crossover operator is used for recombining the best solutions to form two new solutions. Crossover is performed with two parent solutions to form two new child solutions. Crossover is done within priorities. Multi-point crossover is applied at random sites for each priority as shown in Fig. 3. Child 1 is formed by joining the first part of parent 1 and second part of parent 2. Whereas for child two the procedure is done vice versa.

Task Priority 1					Task Priority 2					Task Priority			
		C	rosso	ver sit	e 1		Cross	over s	site 2	Cr	ossove	er site	3
	T_1^1	T_2^1	T_3^1	T_4^1	T_5^1	T_{1}^{2}	T_{2}^{2}	T_{3}^{2}	T_{4}^{2}	T_{1}^{3}	T_{2}^{3}	T_{3}^{3}	T_{4}^{3}
Parent 1	R_4	R ₁	R ₃	R_5	R_1	R_5	R_1	R_2	<i>R</i> ₁	R_4	R_1	R_2	R ₅
	R_1	R_2	R_4	R_3	R_2		R_5	R_4		R_1			R ₃
	T_1^1	T_2^1	T_3^1	T_4^1	T_5^1	T_{1}^{2}	T_{2}^{2}	T_{3}^{2}	T_{4}^{2}	T_{1}^{3}	T_{2}^{3}	T_{3}^{3}	T_{4}^{3}
Parent 2	R_1	R_3	R_5	R_1	R_3	R_2	R_1	R_5	R_1	R_1	R_2	R_5	R_4
	R_2	R_4	R_1	R_4	R_5		R_4	R_1		R_3			R_1
				ŧ			,	ŧ				•	
	T_1^1	T_2^1	T_3^1	T_4^1	T_5^1	T_{1}^{2}	T_{2}^{2}	T_{3}^{2}	T_{4}^{2}	T_{1}^{3}	T_{2}^{3}	T_{3}^{3}	T_4^3
Child 1	R_4	R_1	R ₃	R_1	R_3	R_5	R_1	R_5	R_1	R_4	R_1	R_5	R_4
	R_1	R ₂	R_4	R_4	R_5		R_5	R_1		R_1			R_1
	T_1^1	T_2^1	T_3^1	T_4^1	T_5^1	T_{1}^{2}	T_2^2	T_{3}^{2}	T_4^2	T_{1}^{3}	T_2^3	T_{3}^{3}	T_4^3
	11	12	13	14	15	11	12	13	14	11	12	13	14
Child 2	R_1	R_3	R_5	R_5	R_1	R_2	R_1	R_2	R_1	R_1	R_2	R_2	R_5
	R_2	R_4	R_1	R_3	R_2		R_4	R_4		R_3			R ₃

Figure 3. Crossover procedure.

4.4 Mutation

Crossover operator enables the algorithm to choose better children by swapping of a set of genes at the crossover point, but it cannot change the individual gene of a chromosome, Whereas Mutation alters the specific genes. The mutation procedure isolates the robots assigned to the task in set A, and the remaining robots to another set B. Each element in set A is swapped with a randomly selected element in Set B. Swaps are subjected to mutation probability. If the task requires all the robots, then Set B will be a null set, and hence mutation has no meaning.

4.5 Optimal Level Selection for GA Parameters

The solution quality of the GA depends on operating

Table 1. GA parameters and their levels

Tanala		Para	meters	
Levels	n_p	$\mathcal{P}_{\mathcal{C}}$	$\mathcal{P}_{\!\mathcal{M}}$	n_G
Level 1	25	0.6	0.01	50
Level 2	50	0.7	0.03	100
Level 3	75	0.8	0.05	150

parameters $n_{\mathcal{P}}$, \mathcal{P}_{C} , $\mathcal{P}_{\mathcal{M}}$, and n_{G} . To study the effect of parameters on the solution and to identify the best levels for the parameter, the following experimental design has been constructed. The parameters are at three levels each as given in Table 1. L₉ Orthogonal Array (OA) is a standard array suitable for a analysing the effect of 4 factors with three levels. The maximum number of columns available in standard L₉ OA is 4. The columns in L₉ OA are sufficient enough to accommodate only four factors and interaction between factors cannot be accommodated. In order to analyse the interaction effects, additional columns are required. Hence, L₂₇ OA is chosen to accommodate all the four main factors and two interactions effects.

A pilot run of experiments was conducted using the above levels, and the effect of GA parameters is studied. Table 2

shows the sample ANOVA for performing 20 tasks with 15 robots. Statistical analysis reveals that $\mathcal{P}_{\mathcal{M}}$ and $n_{\mathcal{G}}$ are the most significant factors with a contribution percentage of 66.57 per cent and 20.85 per cent, respectively. All the other factors are insignificant.

The OA based experiments were performed with the different robot to task ratios to check whether the change affects the levels of GA parameters. Table 3 summarises the optimal levels for GA parameters for the various robot to task ratios. Also, it shows that the level 1 (0.01) for \mathcal{P}_M and level 3 (150) for n_G being chosen as the best level for the different robot to task ratios. The optimal levels obtained matches with the work done by Khuntia²⁶, *et al.* for multirobot task allocation.

4.6 Genetic Algorithm-Pseudo Code

The pseudo code for the GA is presented below, and Fig. 4 shows the sample convergence plot based on the

Table 2. Analysis of variance (ANOVA) table

Factor	SS	DOF	μ_{SS}	F_{Calc}	F _{tab}	Contribution (per cent)	Significance
$n_{\mathcal{P}}$	0.04	2.00	0.02	3.29	4.10	3.50	No
$\mathcal{P}_{\mathcal{C}}$	0.01	2.00	0.01	0.97	4.10	1.03	No
$\mathcal{P}_{\!\mathcal{M}}$	0.83	2.00	0.42	62.59	4.10	66.57	Yes
n _G	0.26	2.00	0.13	19.61	4.10	20.85	Yes
$n_{\mathcal{P}} \ge n_{G}$	0.02	4.00	0.00	0.68	3.47	1.45	No
$\mathcal{P}_{\mathcal{M}} \ge n_{G}$	0.02	4.00	0.00	0.61	3.47	1.29	No
Error	0.07	10.00	0.01			5.31	
Total	1.25	26.00				100.00	

fitness value.

// Input $n_{\mathcal{R}}, n_{\mathcal{T}}, \mathcal{D}_k, n_{\mathcal{P}}, n_G, \mathcal{P}_{\mathcal{M}}, \mathcal{P}_{\mathcal{C}}$ //Generate Initial Population Set i=1 Repeat Generate a Random Chromosome C (i) i = i + 1Until $(i! = n_p)$ // Evaluation of Initial Population Set i=1Repeat Calculate $f_n(j)$ for C(j)j=j+1Until $(j! = n_p)$ // Mating Pool Formation Sort C (i) descending based on f_{i} (j) Save C(1) as the Best For m=1 to 10

M(m) = C(m)

End For

// Generation Loop

Set x=0

Repeat

//Crossover
Set $k=0$
For $P=1$ to 10

For Q = P+1 to 10 *Child C (k) & C (k+1) = C(P)*

XC(Q)

k=k+2End For End For Calculate C (k) Sort C (k) descending based on $f_n(k)$ Save C (1)as the Best

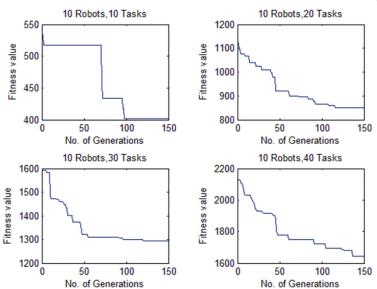


Figure 4. Convergence plot for the different n_{R} and n_{T} .

//Mutation Perform gene wise Mutation C(k)Calculate $f_n(k) C(k)$ Sort C(k) descending based on $f_n(k)$ Save C(1) as the Best //Replacing the Mating pool population For k, P=1 to 10 C(P) = C(k)End For Until (x= n_G)

//Display Results

Table 3.	Percentage contribution (% C) and optimal levels
	(L) for different task sizes

n _R	n _T	n _P		$\mathcal{P}_{\mathcal{C}}$		$\mathcal{P}_{\!_{\mathcal{M}}}$		n _G	
		% C	L	% C	L	% C	L	% C	L
20	10	5.81	3	6.82	2	23.26	1	29.8	3
20	20	1.13	2	0.33	1	65.23	1	23.72	3
20	30	0.2	3	1.1	3	81.99	1	7.91	3
20	40	0.99	3	0.37	1	85.02	1	4.55	3

5. RESULTS AND DISCUSSION

The change in the $n_{\mathcal{R}}$ allocated to a set-of-tasks affects the performance measures of the entire system. When the number of robots is more than the required level, an increase in average idle time per robot (μI_i^R) is seen, which is undesirable. A smaller $n_{\mathcal{R}}$ than the necessary level increases the Average task completion time (μC_i^T) , Average waiting time per robot $(\mu W_i^{\mathcal{R}})$, and average travel per robot $(\mu T_i^{\mathcal{R}})$. So, for a given task level it is essential to identify the optimal number of robots required to complete it. A tradeoff between $\mu \mathcal{I}_i^{\mathcal{R}}$ and $\mu \mathcal{C}_i^T$, $\mu W_i^{\mathcal{R}}$, $\mu T_i^{\mathcal{R}}$ is done to determine the optimal $n_{\mathcal{R}}$ required to complete the tasks. Table 4 presents the results obtained by varying $n_{\mathcal{R}}$ for a given set-of-tasks at different levels.

Refer Fig. 5(a). On plotting the average waiting time per robot against the varying $n_{\mathcal{R}}$ and $n_{\mathcal{T}}$, the following was observed. $\mu W_t^{\mathcal{R}}$ increases for the increase in $n_{\mathcal{T}}$ keeping the $n_{\mathcal{R}}$ constant and decreases for the increase in the $n_{\mathcal{R}}$ for a given $n_{\mathcal{T}}$. Similarly (refer Fig. 5(b).) $\mu \mathcal{I}_t^{\mathcal{R}}$ increases with increase in $n_{\mathcal{R}}$ keeping the $n_{\mathcal{T}}$ constant.

The tradeoff chart for performance measures corresponding to different task levels is as shown in Fig. 6. The optimal n_{π} for the most of the cases are found to be varying between 10 and 15 and occurs at 20 per cent of performance measures. There should be a proportionate increase in the n_{π} for the corresponding increase in the n_{τ} required for 10 and 40 tasks. The reason lies in the inability in the allocation of the robots to the waiting task due to the prioritisation of tasks before completing the preceding ones. In fact, removing the precedence constraints would increase the optimal n_{π} for the corresponding n_{τ} .

$n_{\mathcal{R}} - n_{\mathcal{T}}$	f_t	Performance measures in (time units)							
		C_t^T	$T_t^{\mathcal{R}}$	$\mathcal{W}_{t}^{\mathcal{R}}$	$\mathcal{I}^{\mathcal{R}}_{t}$				
5R-10T	465.11	320.22	1201.28	338.96	0				
10R-10T	401.46	169.24	1085.23	261.95	313.03				
15R- 10 T	490.79	151.78	1152.56	345.79	1003.67				
20R-10T	586.83	147.14	1050.44	146.08	0.00				
5R-20T	806.23	613.11	2201.51	410.29	324.24				
10R-20T	851.71	360.71	2246.83	475.07	1318.30				
15R-20T	1027.26	307.66	2064.47	418.60	2305.85				
20R-20T	1281.93	265.37	2141.75	414.75	0.00				
5R-30T	1146.43	839.84	3194.11	551.78	583.04				
10R-30T	1294.48	583.18	3244.31	767.38	1491.25				
15R-30T	1551.93	483.55	3253.46	979.44	2825.72				
20R-30T	1871.88	404.07	3084.87	1172.87	0.00				
5R-40T	1587.40	1143.06	4361.25	845.28	324.24				
10R-40T	1642.69	712.85	4271.55	1262.14	1630.55				
15R-40T	1968.02	622.87	4423.62	1195.03	3700.18				
20R-40T	2465.96	560.99	4145.37	1457.30	89.44				

Table 4. Performance measures

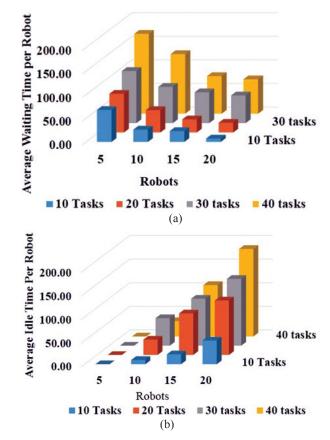


Figure 5. (a) Average waiting time per robot and (b) Average idle time per robot.

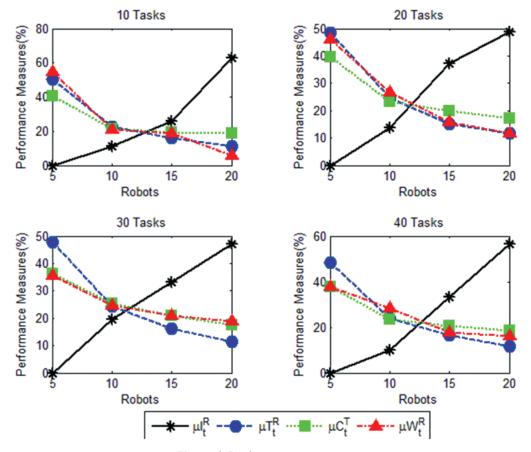


Figure 6. Performance measures.

6. CONCLUSION AND FUTURE SCOPE

The augmented use of autonomous robots in various applications have given rise to the considerable attention of MRTA problem in recent years. This work addresses the allocation of multiple robots to multiple tasks considering four objectives with precedence constraints. The work is aimed to find the best allocation of robots to task and to find the optimal for a given set-of-tasks at any instant of time. GA based methodology was developed to obtain the best allocation of single robots to the multi-robot foraging tasks. Changes in the values of GA parameters have more significant effects on the results. Hence, Taguchi's L_{27} orthogonal array experimental design is used to identify the best values for the GA parameters. It was observed from ANOVA that the Mutation probability and Number of generations are the most significant factors that influence the performance of GA.

The optimal value for the mutation probability (0.01) and the number of generations (150) is unchanged for the different robot to task ratio. The developed methodology was tested by varying the $n_{\mathcal{R}}$ and $n_{\mathcal{T}}$ values, and the results were compared. Though all the objectives are of minimisation type, it is observed that for a fixed number of tasks, $\mu \mathcal{I}_t^{\mathcal{R}}$ increases with a decrease in $\mu \mathcal{C}_t^{\mathcal{T}}$, $\mu \mathcal{W}_t^{\mathcal{R}}$, and $\mu \mathcal{I}_t^{\mathcal{R}}$ for an increase in $n_{\mathcal{R}}$ from 5 to 20. On plotting these performance measures, the tradeoff occurs at almost 20% for all the cases, and the optimal $n_{\mathcal{R}}$ varies from 10 to 15. Also, observed that the precedence constraints limit the use of robots beyond a certain level and hence, the idle time increases with the addition of robots more than the required number.

This work can be extended to different applications by fixing appropriate weights for each of the objectives as per the application requirements and using different methods. Also, the performance of the algorithm may be tested by scaling up the n_R and n_T to a greater extent and comparing it with existing market-based approaches.

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