1. INTRODUCTION

Every language has got some inherent characteristics in terms of occurrences of letters out of the alphabet set in words, which in turn constitutes sentences. Each language has got its own grammar, which defines the constraints on word spellings and syntax of sentences. In each language there are some “vowel” like letters whereas others are “consonant” like, which are basically characterised by the phonetic properties.

The language English has five vowels (‘Y’ also treated sometimes as 6th vowel) and 21 consonants. Some letters such as E, T, O, A, I occur more frequently, whereas others such as B, J, X, W, Z occur occasionally in any given English text. Similarly, there are certain letter combinations such as WX, ZX, BX (diagrams), which are very rare whereas combinations such as TH, ER, HE occur more frequently. Such characteristics and affinity of certain letters with some specific letters makes one language distinguishable from the other and also enables one to check if the given text is meaningful valid plain text of the language or it is a random text (sequence of letters occurring randomly).

While dealing with Cryptography\(^1,2\) one normally processes the text message without word break-up and transforms it to make it unintelligible by destroying the characteristics of the language as described above. But when it comes to crack such coded messages without knowing the key, one needs to check if the text generated out of trials is really developing into meaningful plain text of the language or not. Since word break-up is not known, for such intermediate tests to look for plain texts (solutions), it was felt that an Index can be defined suitably which may differentiate plain texts from random texts of English language. This would be a useful tool for cryptanalysis\(^3\).

An attempt has been made in this direction using fuzzy sets\(^4\) and fuzzy similarity relations\(^5,6\) –an approach normally followed for fuzzy pattern recognition\(^7,8,9\) and classification problems.

One of the main issues related to fuzzy set theoretic approach is to select suitable fuzzy sets (characterising linguistic features), called feature fuzzy sets (FFS). For defining index of garbledness\( (I_g) \) to identify plain English texts, 10 Feature fuzzy sets on 26 character alphabet set of English language have been derived and used as in case of the classification of texts of different regional languages\(^10\) as described below.

2. FEATURE EXTRACTION

2.1 Characteristics of English Language

Every language has got certain characteristics, which can be taken as its signature. Similarly, English language also has certain characteristics\(^12\). Some of these characteristics are as under:

1. All the letters of English are not used equally. Some letters are used very frequently whereas others are used rarely.
2. Most prominent crests in the frequency graph of letters appear at E, T, O, A, N, I, R, S and most prominent troughs are marked at the letters J, K, Q, X, Z.
3. Vowels constitute nearly 40 per cent of the texts with average gaps between these to be 2.5
4. All vowels except U are high frequent letters.
5. Vowels have more affinity to contact consonants than vowels themselves.
6. Consonants have more affinity to contact vowels than consonants themselves.
7. Vowels contact with wide variety of letters.
8. Letters contacting low frequent letters are mostly vowels.
9. Most frequent reversals (XY.... YX) have one vowel and one consonant.
10. The contact of letters on right and left are different for different letters.
11. Some letters form doublets whereas others never occur twice in a sequence.

2.2. Fuzzification of Characteristics of English Language

For 26-character normal texts, the feature fuzzy sets (FFS) are defined on the basic set \( F = \{ A, B, C, \ldots Z \} \) of 26-characters with membership values to be defined suitably which must capture the above mentioned characteristics of English language. The following fuzzy sets based on characteristics of a given text have been chosen as FFS.

2.2.1 Fuzzy Features
The fuzzy sets are defined below:
(1) Number of occurrences of letters.
(2) Very high, high, medium, low and very low categorisation of occurrences of letters.
(3) High occurrences of doublets of the letters.
(4) High occurring diagraphs starting with a letter.
(5) High occurring diagraphs ending with a letter.
(6) Wide variety of left contacts of a letter.
(7) Wide variety of right contacts of a letter.
(8) Wide variety of two-sided contacts of a letter.
(9) Occurrence of the letter with which highest diagraph starting with a given letter is formed.
(10) Occurrence of the letter with which highest diagraph ending with a given letter is formed.

For all these, fuzzy sets on the set \( F \) of 26 letters are suitably constructed by defining characteristic values in \([0, 1]\). In case of (1) above, the normalisation of frequencies by dividing them by the highest frequency brings down the value in \([0, 1]\). Thus

\[
\mu_1(x) = \frac{freq(x)}{\text{Highest freq of single letters}}
\]

However, in case of (2) above, the characteristics have been defined intuitively by the following expressions:

\[
\mu_2(x) = \begin{cases} 
0.1 & \text{if } \mu_1(x) < 0.05 \\
0.2 & \text{if } 0.05 \leq \mu_1(x) < 0.1 \\
0.4 & \text{if } 0.10 \leq \mu_1(x) < 0.2 \\
0.6 & \text{if } 0.20 \leq \mu_1(x) < 0.4 \\
0.8 & \text{if } 0.40 \leq \mu_1(x) < 0.9 \\
1.0 & \text{if } 0.90 \leq \mu_1(x)
\end{cases}
\]

For constructing fuzzy sets corresponding to (3), (4) and (5) above, the corresponding frequencies of the diagraphs have been divided by the highest single letter frequency, since no diagraph frequency can exceed this number. Similarly, the characteristic values corresponding to (6), (7) and (8) are obtained by dividing the number of different letters with which a specific letter is contacting (right, left or two-sided) by 26 as that is the highest value for variety of contacts. Lastly, for fuzzifying (9) and (10) as listed above, the highest single letter frequency is used as normaliser.

Thus, ten fuzzy sets characterising the given text from which these have been extracted are formed. It can be noted that though in the above fuzzy sets, the vowels have not been identified exclusively, the fuzzy sets expressing different kinds of diagraphic patterns implicitly take care of the affinity of some letters (vowels) with other letters. However, the difference and identification of vowels can further be exploited by working out the confidence factors (CFs) of the following occurrences using trapezoidal kind of fuzzy sets on the interval 0-100, as described below:

2.2.2 Intervals of Occurrences of Vowels and Consonants

Based on the statistics of English language, a general pattern of occurrence of vowels and consonants in plain English texts is as follows:

<table>
<thead>
<tr>
<th>Percentage of occurrence of</th>
<th>Interval percent</th>
</tr>
</thead>
<tbody>
<tr>
<td>(a) Vowels</td>
<td></td>
</tr>
<tr>
<td>(i) A, E, I, O, U</td>
<td>35-45</td>
</tr>
<tr>
<td>(b) Consonants</td>
<td></td>
</tr>
<tr>
<td>(ii) T, S, R, N, H</td>
<td>30-40</td>
</tr>
<tr>
<td>(iv) J, K, Q, W, X, Z</td>
<td>0-5</td>
</tr>
</tbody>
</table>

The confidence factors for all these four percentages can be worked out using the general form of trapezoidal type of fuzzy set, as shown in Fig. 1.
Mathematically,
\[
\mu_m(x) = \begin{cases} 
1 & \text{if } a \leq x \leq b \\
\frac{3a-b-2x}{a-b} & \text{if } \frac{3a-b}{2} \leq x \leq b \\
\frac{3b-a-2x}{b-a} & \text{if } b \leq x \leq \frac{3b-a}{2} \\
0 & \text{elsewhere}
\end{cases}
\]

For (i) to (iv) above, \(a\) and \(b\) are chosen as the given intervals and confidence factors (CF) can be calculated. These CF’s will be combined with the index obtained through the 10 FFSs to work out the combined index, as described below.

3. **INDEX FORMULATION**

3.1 **Similarity Fuzzy Relation and Dissimilarity Measure**

For the comparison of two fuzzy sets, \(\mu_1\) and \(\mu_2\), different kinds of fuzzy relations can be used. For our purpose, the following two fuzzy relations were considered:

\[
\mu_x(x,y) = \frac{k}{k + |\mu_1(x) - \mu_2(y)|}
\]

\[
\mu_y(x,y) = e^{-|\mu_1(x) - \mu_2(y)|}
\]

(1)

where \(k\) and \(l\) are parameters that can be suitably chosen\(^{11}\), \(\mu_1(x)\) and \(\mu_2(y)\) represent membership values corresponding to plain text and the given text, respectively. Both of these give almost similar kinds of results except scaling. Hence the first one has been used in designing the present system, the parameters \(k\) and \(l\) have been adjusted through learning by providing the system different plain English texts of varying lengths. The values finally fixed up are \(k = 0.7\) and \(l = 2\). This fuzzy similarity relation induces a \(26 \times 26\) fuzzy similarity matrix \(R\) with entries from \([0,1]\). These have 10 such fuzzy similarity matrices corresponding to the 10 characteristics considered in Section 2.1. The following measure of dissimilarity\(^{18}\) has been used:

\[
D = \alpha(26 - \text{Trace } R) + \beta \sum \left( \mu_x(x,y) - \mu_y(y,x) \right)
\]

(2)

where the \(\Sigma\Sigma\) infact is nothing but the sum of symmetric differences of entries in the matrix \(R\). Again, here \(\alpha\) and \(\beta\) are some parameters, which can be learnt through known examples. In the present case, \(\alpha\) and \(\beta\) were fixed up as 1 and 0.3, respectively. These values were adjusted through learning process using known plain texts of different lengths.

3.2 **The Algorithm and Decision Process**

**Part I**

The extraction and stabilisation of characteristic values of various fuzzy sets for clear English texts was the first problem. The values change with length and are never fixed in two texts. Therefore, for fairly faithful prototyping, quite a large number of plain English texts of various lengths (200 – 400 characters) were run and the fuzzy sets (all 10 say \(P_1, P_2, \ldots, P_{10}\)) were calculated. The variations in characteristic values were studied. Based on these, some standard prototype fuzzy sets were constructed which are used in the Part II of the algorithm.

**Part II**

This module is the main module for the calculation of Index of Garbledness \((I_g)\). A given text (whatever it may be) as a continuous string of characters is passed to this module and all 10 fuzzy sets \(C_1, C_2, \ldots, C_{10}\) are constructed in the specified manner as already pointed out. Now the question comes to compare these with the corresponding fuzzy sets \(P_1, P_2, \ldots, P_{10}\) prototyped for plain English texts in first **Part I**.

For each \(i = 1, \ldots, 10\) : \(\mu_1 = P_i\) and \(\mu_2 = C_j\) and the fuzzy similarity relation (1) is applied to calculate a \(26 \times 26\) fuzzy similarity matrix \(R^{(i)}\). Using the expression in (2), dissimilarity measures defined as

\[
D_i = \alpha(26 - \text{Trace } R^{(i)}) + \beta \sum (R^{(i)}(j,k) - R^{(i)}(k,j))
\]

are calculated. These give the distances of individual characteristics present in the text under scrutiny. But these have to be combined to arrive at an index which can measure the garbledness present in the text. Just averaging was tried first but that does not give good results. Therefore, a weighted average was considered suitable. Again the weights were adjusted through the outcomes of known examples and were fixed up as follows:

<table>
<thead>
<tr>
<th>(w_1)</th>
<th>(w_2)</th>
<th>(w_3)</th>
<th>(w_4)</th>
<th>(w_5)</th>
<th>(w_6)</th>
<th>(w_7)</th>
<th>(w_8)</th>
<th>(w_9)</th>
<th>(w_{10})</th>
</tr>
</thead>
<tbody>
<tr>
<td>(0.142)</td>
<td>(0.132)</td>
<td>(0.031)</td>
<td>(0.093)</td>
<td>(0.093)</td>
<td>(0.115)</td>
<td>(0.115)</td>
<td>(0.093)</td>
<td>(0.093)</td>
<td>(0.093)</td>
</tr>
</tbody>
</table>

The total dissimilarity was thus calculated as

\[
D = \sum_{i=1}^{10} w_i D_i
\]

This \(D\) has been combined with the confidence factors of the text being plain in terms of various percentages of vowels and consonants as discussed earlier. For correct plain texts, it is expected that all the four confidence factors \(CF_1, CF_2, CF_3, \text{ and } CF_4\) will have highest value 1, since the four percentages (vowels, high, medium and low consonants) will lie in the admissible interval. Thus the dissimilarity due to these factors could be measured by

\[
DP = 4 \cdot (CF_1 + CF_2 + CF_3 + CF_4)
\]

and the final index of garbledness present in the text has been defined as

\[
I_g = D + DP
\]

The value of \(I_g\) gives an indication about the garbledness present in the text.

4. **RESULTS**

The algorithm developed has been tested on a number of English texts of various types namely plain text, partially-garbled text (garbledness between 10 per cent and 50 per
cent and between 50 per cent and 90 per cent), and totally-garbled text. Partially-garbled texts are prepared by replacing some of the characters in the plain-text by other characters. Preparation of totally-garbled text has been done by encryption of the plain-text with simple substitution scheme. Working of this algorithm is explained by the following examples.

4.1 Working of the Tool Developed for $I_g$

Example I:
Plain Text:

eilandmatungasien thehistoryofthisgroupofislandslocated on thewestcoastofIndiagoeswaybacktothestoneagegeo
eimptementshavebeenfoundateveralitiesitheseislands heoc
toalregionsandsupremuslytheislands werethomeofthe
tolifisgerolkind possessesdistantpastinthistorybetheislandsw
erowering themagadhanempireunderemperorashokaafterhis
dearththeislandsgangedhandsfromonekingtoanotherfortw
othousandyears theybelonged to.

Values of the corresponding 10 $D_i$'s are:
$D_1 = 1.01, \quad D_2 = 1.28, \quad D_3 = 0.00, \quad D_4 = 0.33,$
$D_5 = 0.35, \quad D_6 = 0.68, \quad D_7 = 0.76, \quad D_8 = 0.73,$
$D_9 = 2.02, \quad D_{10} = 2.59$

Value of $D = \sum_{i=1}^{10} w_i D_i = 9.75$

Values of 4 confidence factors ($CF_i$'s, $i = 1, 2, 3, 4$) are:
$CF_1 = 1.00, \quad CF_2 = 1.00,$
$CF_3 = 1.00, \quad CF_4 = 1.00$

Value of DP ($= 4-((CF_1^2 + CF_2^2 + CF_3^2 + CF_4^2))$) = 4.00
Hence value of $I_g (=D + DP) = 9.75$

Example II:
Partially-garbled Text:

Values of the corresponding 10 $D_i$'s are:
$D_1 = 3.17, \quad D_2 = 3.18, \quad D_3 = 0.00, \quad D_4 = 0.45,$
$D_5 = 0.48, \quad D_6 = 1.94, \quad D_7 = 1.83, \quad D_8 = 2.10,$
$D_9 = 4.19, \quad D_{10} = 3.83$

Value of $D = \sum_{i=4}^{10} w_i D_i = 21.17$

Values of 4 confidence factors ($CF_i$'s, $i = 1, 2, 3, 4$) are:
$CF_1 = 0.80, \quad CF_2 = 1.00,$
$CF_3 = 0.70, \quad CF_4 = 0.00$

Value of DP ($= 4-((CF_1^2 + CF_2^2 + CF_3^2 + CF_4^2))$) = 1.50
Hence value of $I_g (=D + DP) = 22.67$

Example III:
Totally-garbled Text (a cryptogram):
kjwptzwoplsqgrdkqsrqgcrqngfrdpslurgygnqsjwptsgxw
rtgpkrddklkxskrsxwgrqntpqwlkgwceweargdskrgpklnssrg
pkwlkqzyjzksprsdwmeekkpqpgoptwrskmkuwjsqapsqgrdks
kqjwptdksxwgrjkuqlqgswptuykszwejerdqsjwptshk
krdkdqgzkngdrgqnsqdkingqaurqdpqswiywswprqgqtk
prouceqrdskqswqjkpsvptshkhkywurgnrdkrzwvldwpzpsqkopt
kyzykugwsgrrqtsqkmsrwdqkrsjwptxwdprktdwptsmtu
pglpqklpqgrwprgksqfngurgrdsogwptkweurdkkek

Values of the corresponding 10 $D_i$'s are:
$D_1 = 5.19, \quad D_2 = 4.74, \quad D_3 = 0.00, \quad D_4 = 0.52,$
$D_5 = 0.51, \quad D_6 = 2.39, \quad D_7 = 2.26, \quad D_8 = 2.59,$
$D_9 = 3.66, \quad D_{10} = 3.37$

Value of $D = \sum_{i=1}^{10} w_i D_i = 25.25$

Values of 4 confidence factors ($CF_i$'s, $i = 1, 2, 3, 4$) are:
$CF_1 = 0.00, \quad CF_2 = 0.40,$
$CF_3 = 0.00, \quad CF_4 = 0.00$

Value of DP ($= 4-((CF_1^2 + CF_2^2 + CF_3^2 + CF_4^2))$) = 3.60
Hence value of $I_g (=D + DP) = 28.85$

It may be observed that out of four $CF_i$'s, three are zero in the present example. This is due to the fact that the text here is a cryptogram based on a simple encryption scheme and hence is not as random as it would be in case of strong encryption schemes. In that case even $CF_i$'s are all non-zero and index $I_g$ goes up further.

The s/w based on this algorithm has been tested on 125 text files from each category of plaintext, partially garbled text and totally garbled text. Each text file has 400 characters. It is observed that in case of plain English texts, the value of this index is below 19. But in case of crypts and totally garbled texts, it is between 23 and 32. For texts having some plain text and some garbage (i.e. partially garbled text), the value of $I_g$ in most of the cases is in between 19 and 23 and measures the plain text characteristics relatively present in the text i.e. the value of $I_g$ gives an indication about the garbledness present in the text.

5. CONCLUSIONS

The index of garbledness ($I_g$) developed works very well for identification of plain English text. Therefore, it can be used for identification of the solution while going for exhaustive trial, especially in those systems where either the correct text is formed during a key trial or it is totally garbled. Even in case of cryptosystems, where partial texts could be formed by a key trial, the value of $I_g$ indicates the degree to which the correct solution has been formed and thus may give a hint to the next key for trial in certain cases. Thus this $I_g$ could be used for directed search of the reduced key space instead of sequential search. The value of $I_g$ is also a powerful tool for fitness
functions in case of genetic algorithms for cryptanalysis, which would help in selection of new generations from the old ones.

REFERENCES

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